

ST512 - Lab 10 - Osborne

1. (Exercise taken from p. 685 of Rao's "Statistical Research Methods in the Life Sciences"):

- See data file called "wether.dat"
- Study investigates three diet supplements on weights of wethers (rams)
- Four randomly selected locations(i.e. environments)
- 24 wethers randomly assigned to locations in a balanced design
- In each location, all three diets used, two animals per diet.

(a) Propose a model for these data: $Y_{ijk} = ?$

- Fixed, random or mixed?
- Nested or crossed?

(b) Obtain two scatterplots with mean weight gain on the vertical axis and:

- location on the horizontal axis with different symbols for different diets
- diet on the horizontal axis with different symbols for different locations

```
symbol1 i=join value=dot;
```

```
proc means nway noprint; /* nway suppresses marginal means */  
  class diet location;  
  vary y;  
  output out=two mean=ymean;  
run;
```

```
proc gplot;  
  plot ymean*location=diet;  
  plot ymean*diet=location;  
run;
```

(c) Inspect the plots

- Does the first plot provide evidence of a location effect?
- a location \times diet effect?
- Does the second plot provide evidence of a diet effect?
- a location \times diet effect?

(d) Investigate these effects by fitting a two-factor model with interaction using PROC GLM. Note that if the location effect is random, the p -values from F -tests may not be right.

(e) Further investigate these effects by fitting a mixed model using the code below:

```
proc mixed method=type3;
  class location diet;
  model wtgain=diet/ddfm=satterth;
  random location location*diet;
run;
```

- i. Find the correct F -ratio and p -values to test for
 - A. A random diet \times location interaction effect
 - B. A random location effect
 - C. A fixed diet effect
- ii. Find the estimated variance components which quantify the magnitude of the first two of these effects above (d)iA (d)iB.
- iii. For each of the three variance components, obtain Wald 95% confidence intervals of the form

$$\left(\frac{\hat{d}f \hat{\sigma}_x^2}{\chi_{df}^2(0.025)}, \frac{\hat{d}f \hat{\sigma}_x^2}{\chi_{df}^2(0.975)} \right)$$

using the `c1` option in the `proc mixed` statement:

```
proc mixed c1; /* without method=type3 option */
```

- iv. As in problem 14.16d, obtain simultaneous 90% confidence intervals for all 3 pairwise differences of diet means. (Satterthwaite formula for $\hat{d}f$ associated w/ SE terms is unnecessary here.)

```
lsmeans diet/adj=bon c1 alpha=0.1;
```

Conclusion: though there is evidence of a diet \times location random interaction effect, so that the random location effects vary by diet, the diet main effect is not significant and none of the pairwise comparisons among diet means are significant, thus not providing much evidence of a fixed diet effect. Averaged over locations, mean weight gain is plausibly equal for the diets.